

# MA202 Exam 4 Review Solutions

- 1) a) True. Write  $n$  as  $\frac{n}{1}$ . b) True. This is the defining property of rational numbers.  
 c) False. Negative rationals can't be. d) True. Same reason as a).  
 e) False.  $\frac{1}{3} = 0.3333\dots$  f) True, by definition.

	$\mathbb{N}$	$\mathbb{Z}$	$\mathbb{Q}$	not rational	$\mathbb{R}$
$\frac{1}{3}$	X	X	✓	X	✓
$\sqrt{5}$	X	X	X	✓	✓
$-\sqrt{4}$	X	✓	✓	X	✓
0	X	✓	✓	X	✓
$-5/4$	X	X	✓	X	✓
$2.\bar{3}$	X	X	✓	X	✓
$2\pi$	X	X	X	✓	✓

3) 0, since  $0 + (-0) = 0$ .

4) Lots: ~~many~~,  $\sqrt{2}, \sqrt{3}, \sqrt{5}, \sqrt{7}$

5) We need to know how much longer we run each day.

6)  $13 + \frac{n}{48} = 21$

$\frac{n}{48} = 8$

$n = 48 \cdot 8 = \boxed{384}$

7) a) True.  $90^\circ + 90^\circ = 180^\circ$ .

b) Sometimes. ~~40~~  $60^\circ + 30^\circ = 90^\circ$ , but  $40^\circ + 20^\circ \neq 90^\circ$ .

c) Sometimes. but .

d) Never. Two angles of any triangle are not supplementary because then the third angle would be  $0^\circ$ .

e) Sometimes. ~~120 and 60 are~~

Never. Adding two numbers greater than 90 gives a number greater than 180.

f) Sometimes. True for  $120^\circ$  and  $60^\circ$ , false for  $90^\circ$  and  $90^\circ$ .

g) True, since the right angle is  $90^\circ$  and all three sum to  $180^\circ$ .

h) Never. The acute ~~the~~ angles of an obtuse triangle sum to less than ~~to~~  $90^\circ$ .

8) a) Sometimes, if it is a square.

b) Always. In order to have two parallel sides, a quadrilateral must be convex.

c) Sometimes, if it is a rectangle.

d) Sometimes, not for all.

e) Never. Parallel lines do not intersect.

9) a)  $180(n-2)^\circ$

b)  $\frac{180(n-2)^\circ}{n}$ . Since the regular  $n$ -gon

has  $n$  angles and they sum to  $180(n-2)$ ,

each must measure  $\frac{180(n-2)}{n} = (180 - \frac{360}{n})^\circ$

c) Only triangles, squares, and hexagons.

All other regular  $n$ -gons have angle measures that do not divide  $360^\circ$ , so there will be a gap (overlap) in the attempted tessellation.

10)  $24 \text{ fl. oz.} \cdot \frac{1}{10} \cdot \frac{1 \text{ cup}}{8 \text{ fl. oz.}} \cdot \frac{1 \text{ gal}}{16 \text{ c}} \cdot \frac{1 \text{ L}}{0.26 \text{ gal}} \approx \boxed{0.43 \text{ L of water}}$

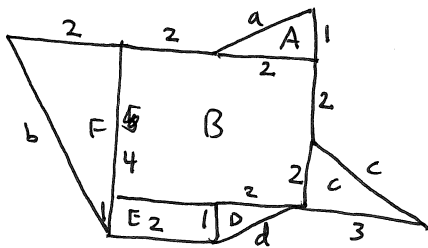
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11)  $\frac{3}{4} \text{ gal.} \cdot \frac{1 \text{ batch}}{1 \text{ gal.}} \cdot \frac{1 \text{ batch}}{\frac{1}{4} \text{ cup}} = \boxed{48 \text{ batches}}$

12] a)  $d = \overset{\text{rate}}{v} \cdot \underset{\text{time}}{t}$   $d = (340 \frac{\text{m}}{\text{s}})(24\text{s}) \cdot \frac{1\text{km}}{1000\text{m}} = 8.16 \text{ km}$

b)  $d = vt \rightarrow 1 \text{ mi} \approx 1.61 \text{ km} \rightarrow 1610 = (340 \frac{\text{m}}{\text{s}})t$   
 $= 1610 \text{ m}$   
 $t \approx \frac{1610}{340} \approx \boxed{4.74 \text{ s}}$

13]



For perimeter, use Pyth. Thm to find a, b, c, d.

$$2^2 + 5^2 = b^2 \Rightarrow b = \sqrt{29}$$

$$1^2 + 2^2 = a^2 \Rightarrow a = d = \sqrt{5}$$

$$2^2 + 3^2 = c^2 \Rightarrow c = \sqrt{13}$$

$$P = \sqrt{5} + 3 + \sqrt{13} + 3 + \sqrt{5} + 2 + \sqrt{29} + 4$$

$$= \boxed{12 + 2\sqrt{5} + \sqrt{13} + \sqrt{29} \text{ units}}$$

For area, find A, B, C, D, E, F and add:

$$A = \frac{1}{2}(1)(2) = 1 \quad B = 4 \cdot 4 = 16 \quad C = \frac{1}{2}(2)(3) = 3 \quad D = \frac{1}{2}(1)(2) = 1 \quad E = (1)(2) = 2 \quad F = \frac{1}{2}(2)(5) = 5$$

$$\text{Area} = 1 + 16 + 3 + 1 + 2 + 5 = \boxed{28 \text{ units}^2}$$